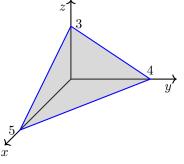
## $\Re$ eview Questions -1

- 1. Find  $|\vec{u} + \vec{v}|$  if  $\vec{u} = \langle 2, -1, 1 \rangle$  and  $\vec{v} = \langle -1, 3, 13 \rangle$ .
- 2. Determine whether the vectors  $\vec{u} = \langle 1, 2, 2 \rangle$ ,  $\vec{v} = \langle \sqrt{2}, 1, -1 \rangle$  are orthogonal, parallel or neither. If neither, also find the angle between two vectors.
- 3. Find  $\cos \widehat{ABC}$  if A(1,4), B(2,2) and C(3,5). Find the measure of the angle  $\widehat{ABC}$ .
- 4. Find  $\cos \widehat{BCA}$  if A(1,4), B(2,2) and C(3,5). Find the measure of the angle  $\widehat{ABC}$ .
- 5. Find the vector projection  $proj_{\vec{v}}\vec{u}$  if  $\vec{u} = \langle 2, -1 \rangle$  and  $\vec{v} = \langle 1, 3 \rangle$ .
- 6. Find the vector projection  $proj_{\vec{v}}\vec{u}$  if  $\vec{u} = \langle 0, 1, 2 \rangle$  and  $\vec{v} = \langle 1, 1, \sqrt{2} \rangle$ .
- 7. Find  $|\vec{u} \times \vec{v}|$  if  $|\vec{u}| = 5, |\vec{v}| = 6$ , and the angle between  $\vec{u}$  and  $\vec{v}$  is 30°.
- 8. Find symmetric equations of the line through the point  $P_0(-2, 1, 3)$  and parallel to the line  $x = 2 + t, \ y = -1 + 5t, \ z = 4t.$
- 9. Find a vector equation of the line trhough the points A(2,4,3) and B(1,2,-1). Also give parametric equations for the line. Where does the line intersect xz-plane?
- 10. Determine whether the planes 2x + y z = 1 and x + y + 3z = 2 are parallel, perpendicular or neither. If neither, also find the angle between two planes.
- 11. Determine whether the planes  $\sqrt{2}x + y + z = 1$  and  $\sqrt{2}x y + z = 5$  are parallel, perpendicular or neither. If neither, also find the angle between two planes.
- 12. Find the distance from the point P(4,5,6) to the plane 2x y + z = 6.
- 13. Let  $\mathcal{P}$  be the plane containing the point (2, 1, 1) and perpendicular to x-axis. Which of the following sets of equations describes the intersection of the plane  $\mathcal{P}$  with the sphere of radius 3 centered at the origin?
- 14. Let  $\mathcal{P}$  be the plane with equation x + 2y + z = 10 and l be the line through the points A(1, 0, -1) and B(2, 1, 1). Find the point of intersection if they intersect.
- 15. By using triple product, find the volume of the parallelepiped determined by the vectors  $\vec{u} = \langle 0, 2, 1 \rangle$ ,  $\vec{v} = \langle -1, 3, 0 \rangle$  and  $\vec{w} = \langle 2, 1, -1 \rangle$ .

16. Find an equation of the plane containing the given triangle.



- 17. Calculate the dot product  $(\vec{u} + \vec{v}) \cdot (\vec{u} \vec{v})$  if  $\vec{u} = i + 3j + k$ and  $\vec{v} = 5i - j - 2k$ . Is the angle between the vectors  $\vec{u} + \vec{v}$ and  $\vec{u} - \vec{v}$  obtuse or acute? Find the angle between  $\vec{u}$  and  $\vec{v}$ .
- 18. Calculate the cross product  $(\vec{u} + 2\vec{v}) \times (2\vec{u} \vec{v})$  if  $\vec{u} = j + 2k$ and  $\vec{v} = 2i - j + k$ .
- 19. Find the limit  $\lim_{t \to 2} \left\langle t^2, \frac{\sin(t-2)}{t^2-4}, e^t \right\rangle$ .
- 20. For the vector function  $\vec{r}(t) = \langle t^2, \cos t, e^{2t} \rangle$  find the second order derivative when t = 0. In other words,  $\vec{r}''(0) = ?$
- 21. Find the rate of change for vector function  $\vec{r}(t) = \langle \sin t, \cos t, \tan t \rangle$  when  $t = \pi/6$ .
- 22. Determine whether the vector-valued function  $\vec{r}(t) = \left\langle \frac{1}{t+2}, \ln(t-2), t^2 \right\rangle$  is continuous or not at t = 2.
- 23. Find the vector function  $\vec{r}(t)$  if  $\vec{r}'(t) = \langle 2t, \cos t, e^t \rangle$  and  $\vec{r}(0) = \langle 1, 2, 3 \rangle$ .
- 24. Evaluate the integral  $\int_0^1 \left( t \boldsymbol{i} + \frac{2t}{1+t^2} \, \boldsymbol{j} + e^t \boldsymbol{k} \right) dt.$
- 25. The velocity of an object is given by  $\vec{v}(t) = \left\langle 2t, \sin t, \frac{1}{t+1} \right\rangle$  and  $\vec{v}(0) = \langle 1, 1, 1 \rangle$ . Find the position function  $\vec{r}(t)$ .
- 26. Find the length of the curve  $\vec{r}(t) = \langle \sqrt{5}t, \cos 2t, -\sin 2t \rangle$ from t = 0 to  $t = 2\pi$ .
- 27. Find the unit tangent vector  $\vec{T}(t)$  to the curve  $\vec{r}(t) = \langle t, \cos t, \sin t \rangle$  at  $t = \pi/3$ .
- 28. Find the curvature of the function  $\vec{r}(t) = \langle t, t^2, 0 \rangle$  at t = 1.